

3rd Tutorial to
Econometric Methods and Applications WS 2017/18

Exercise 13 [2.5%]

Exercise 6.5 Stock & Watson: Introduction to Econometrics (Third Edition, p.248)

Data were collected from a random sample of 220 home sales from a community in 2003. Let *Price* denote the selling price (in 1000 \$), *BDR* denote the number of bedrooms, *Bath* denote the number of bathrooms, *Hsize* denote the size of the house (in square feet), *Lsize* denote the lot size (in square feet), *Age* denote the age of the house (in years), and *Poor* denote a binary variable that is equal to 1 if the condition of the house is reported as "poor". An estimated regression yields

$$\begin{aligned}\widehat{Price} &= 119.2 + 0.485 \cdot BDR + 23.4 \cdot Bath + 0.156 \cdot Hsize + 0.002 \cdot Lsize \\ &\quad + 0.090 \cdot Age - 48.8 \cdot Poor \\ \overline{R}^2 &= 0.72 \\ SER &= 41.5\end{aligned}$$

- (a) Suppose that a homeowner converts part of an existing family room in her house into a new bathroom. What is the expected increase in the value of the house?
- (b) Suppose that a homeowner adds a new bathroom to her house, which increases the size of the house by 100 square feet. What is the expected increase in the value of the house?
- (c) What is the loss in value if a homeowner lets his house run down so that its condition becomes "poor"?
- (d) Compute the R^2 for the regression.

Exercise 14 [2.5%]

With the linear model

$$\text{wage}_i = \beta_0 + \beta_1 \text{educ}_i + \beta_2 \text{exper}_i + \beta_3 \text{female}_i + \beta_4 \text{married}_i + u_i, i \in \{1, \dots, n\},$$

wages (**wage**) are regressed on years of education (**educ**), years of professional experience (**exper**), a dummy variable for gender (**female**) and a dummy for marital status (**married**).

- (a) The estimation results are (assuming homoskedastic errors):

```
Call:
lm(formula = wage ~ educ + exper + female + married)
```

Residuals:

	Min	1Q	Median	3Q	Max
	-6.4057	-1.9042	-0.5982	1.1454	14.6545

Coefficients:

	Estimate	Std. Error	t value	Pr(> t)
(Intercept)	-1.79066	0.75121	-2.384	0.0175 *
educ	0.58332	0.05166	11.292	< 2e-16 ***
exper	0.05567	0.01106	5.035	6.59e-07 ***
female	-2.06710	0.27221	-7.594	1.45e-13 ***
married	0.66024	0.29685	2.224	0.0266 *

Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

Residual standard error: 3.066 on 521 degrees of freedom

Multiple R-squared: 0.3158, Adjusted R-squared: 0.3105

F-statistic: 60.12 on 4 and 521 DF, p-value: < 2.2e-16

What wages are predicted by the model for

- (i) female singles
- (ii) male singles
- (iii) married women
- (iv) married men

with 15 years of professional experience and 12 years of education?

What is the effect of being married on wages?

- (b) After introducing an interaction term for the two dummy variables ('I(female * married)'), for married women taking the value 1 and being 0 otherwise), the model was re-estimated:

```
Call:
lm(formula = wage ~ educ + exper + female + married + I(female *
  married))
```

Residuals:

	Min	1Q	Median	3Q	Max
	-6.8255	-1.7078	-0.5796	1.0495	14.2206

Coefficients:

	Estimate	Std. Error	t value	Pr(> t)
(Intercept)	-2.65518	0.75492	-3.517	0.000474 ***
educ	0.57811	0.05053	11.441	< 2e-16 ***
exper	0.05322	0.01082	4.918	1.18e-06 ***
female	-0.42373	0.42423	-0.999	0.318346
married	2.08000	0.40707	5.110	4.54e-07 ***

```

I(female * married) -2.70735    0.54416  -4.975 8.87e-07 ***
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Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

Residual standard error: 2.999 on 520 degrees of freedom
Multiple R-squared:  0.3469, Adjusted R-squared:  0.3406
F-statistic: 55.24 on 5 and 520 DF,  p-value: < 2.2e-16

```

What wages are predicted by the model for

- (i) female singles
- (ii) male singles
- (iii) married women
- (iv) married men

with 15 years of professional experience and 12 years of education?

What is the effect of being married on wages for males and females, resp.?

- (c) After introducing a further interaction effect ('I(female * exper)', being equal to 0 for men and giving the years of professional experience for women), the estimation result was:

```

Call:
lm(formula = wage ~ educ + exper + female + married + I(female *
  married) + I(female * exper))

Residuals:
    Min       1Q   Median       3Q      Max
-7.3283 -1.6474 -0.5308  1.0442 14.1439

Coefficients:
                Estimate Std. Error t value Pr(>|t|)
(Intercept)    -3.15376    0.77453  -4.072 5.39e-05 ***
educ             0.59431    0.05063  11.739 < 2e-16 ***
exper           0.08080    0.01506   5.363 1.23e-07 ***
female          0.19589    0.48380   0.405 0.685718
married         1.79901    0.41881   4.296 2.08e-05 ***
I(female * married) -2.22990    0.57107  -3.905 0.000107 ***
I(female * exper)  -0.05335    0.02039  -2.616 0.009154 **
---
Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

Residual standard error: 2.982 on 519 degrees of freedom
Multiple R-squared:  0.3554, Adjusted R-squared:  0.3479
F-statistic: 47.69 on 6 and 519 DF,  p-value: < 2.2e-16

```

What is the effect of an additional year of professional experience for men and women, resp.? Also give an interpretation for the regression coefficient for 'I(female * exper)'.